



2005 AMC 10B

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Question 1

Not yet answered

Points out of 6

A scout troop buys 1000 candy bars at a price of five for 2 dollars. They sell all the candy bars at the price of two for 1 dollar. What was their profit, in dollars?

- (A) 100 (B) 200 (C) 300 (D) 400 (E) 500

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 2

Not yet answered

Points out of 6

A positive number x has the property that $x\%$ of x is 4. What is x ?

- (A) 2 (B) 4 (C) 10 (D) 20 (E) 40

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 3

Not yet answered

Points out of 6

A gallon of paint is used to paint a room. One third of the paint is used on the first day. On the second day, one third of the remaining paint is used. What fraction of the original amount of paint is available to use on the third day?

- (A) $\frac{1}{10}$ (B) $\frac{1}{9}$ (C) $\frac{1}{3}$ (D) $\frac{4}{9}$ (E) $\frac{5}{9}$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 4

Not yet answered

Points out of 6

For real numbers a and b , define $a \diamond b = \sqrt{a^2 + b^2}$. What is the value of

$(5 \diamond 12) \diamond ((-12) \diamond (-5))$?

- (A) 0 (B) $\frac{17}{2}$ (C) 13 (D) $13\sqrt{2}$ (E) 26

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 5

Not yet answered

Points out of 6

Brianna is using part of the money she earned on her weekend job to buy several equally-priced CDs. She used one fifth of her money to buy one third of the CDs. What fraction of her money will she have left after she buys all the CDs?

- (A) $\frac{1}{5}$ (B) $\frac{1}{3}$ (C) $\frac{2}{5}$ (D) $\frac{2}{3}$ (E) $\frac{4}{5}$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 6

Not yet answered

Points out of 6

At the beginning of the school year, Lisa's goal was to earn an A on at least 80% of her 50 quizzes for the year. She earned an A on 22 of the first 30 quizzes. If she is to achieve her goal, on at most how many of the remaining quizzes can she earn a grade lower than an A?

- (A) 1 (B) 2 (C) 3 (D) 4 (E) 5

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 7

Not yet answered

Points out of 6

A circle is inscribed in a square, then a square is inscribed in this circle, and finally, a circle is inscribed in this square. What is the ratio of the area of the smaller circle to the area of the larger square?

- (A) $\frac{\pi}{16}$ (B) $\frac{\pi}{8}$ (C) $\frac{3\pi}{16}$ (D) $\frac{\pi}{4}$ (E) $\frac{\pi}{2}$

Select one:

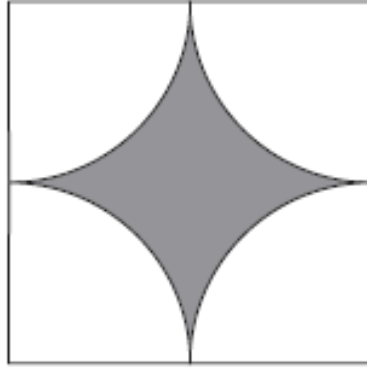
- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 8

Not yet answered

Points out of 6

An 8-foot by 10-foot floor is tiled with square tiles of size 1 foot by 1 foot. Each tile has a pattern consisting of four white quarter circles of radius $\frac{1}{2}$ foot centered at each corner of the tile. The remaining portion of the tile is shaded.



How many square feet of the floor are shaded?

- (A) $80 - 20\pi$ (B) $60 - 10\pi$ (C) $80 - 10\pi$ (D) $60 + 10\pi$ (E) $80 + 10\pi$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 9

Not yet answered

Points out of 6

One fair die has faces 1, 1, 2, 2, 3, 3 and another has faces 4, 4, 5, 5, 6, 6. The dice are rolled and the numbers on the top faces are added. What is the probability that the sum will be odd?

- (A) $\frac{1}{3}$ (B) $\frac{4}{9}$ (C) $\frac{1}{2}$ (D) $\frac{5}{9}$ (E) $\frac{2}{3}$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 10

Not yet answered

Points out of 6

In $\triangle ABC$, we have $AC = BC = 7$ and $AB = 2$. Suppose that D is a point on line AB such that B lies between A and D and $CD = 8$. What is BD ?

- (A) 3 (B) $2\sqrt{3}$ (C) 4 (D) 5 (E) $4\sqrt{2}$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 11

Not yet answered

Points out of 6

The first term of a sequence is 2005. Each succeeding term is the sum of the cubes of the digits of the previous term. What is the 2005th term of the sequence?

- (A) 29 (B) 55 (C) 85 (D) 133 (E) 250

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 12

Not yet answered

Points out of 6

Twelve fair dice are rolled. What is the probability that the product of the numbers on the top faces is prime?

- (A) $\left(\frac{1}{12}\right)^{12}$ (B) $\left(\frac{1}{6}\right)^{12}$ (C) $2\left(\frac{1}{6}\right)^{11}$ (D) $\frac{5}{2}\left(\frac{1}{6}\right)^{11}$ (E) $\left(\frac{1}{6}\right)^{10}$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 13

Not yet answered

Points out of 6

How many numbers between 1 and 2005 are integer multiples of 3 or 4 but not 12?

(A) 501 (B) 668 (C) 835 (D) 1002 (E) 1169

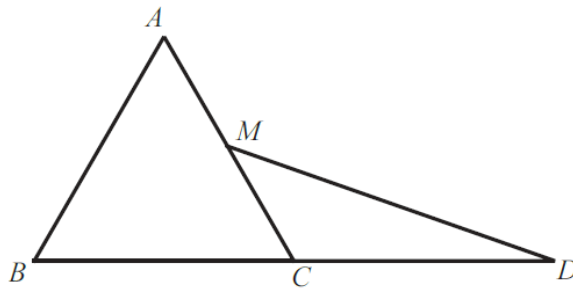
Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 14

Not yet answered

Points out of 6

Equilateral $\triangle ABC$ has side length 2, M is the midpoint of \overline{AC} , and C is the midpoint of \overline{BD} .What is the area of $\triangle CDM$?(A) $\frac{\sqrt{2}}{2}$ (B) $\frac{3}{4}$ (C) $\frac{\sqrt{3}}{2}$ (D) 1 (E) $\sqrt{2}$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 15

Not yet answered

Points out of 6

An envelope contains eight bills: 2 ones, 2 fives, 2 tens, and 2 twenties. Two bills are drawn at random without replacement. What is the probability that their sum is \$20 or more?

- (A) $\frac{1}{4}$ (B) $\frac{2}{5}$ (C) $\frac{3}{7}$ (D) $\frac{1}{2}$ (E) $\frac{2}{3}$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 16

Not yet answered

Points out of 6

The quadratic equation $x^2 + mx + n$ has roots twice those of $x^2 + px + m$, and none of m , n , and p is zero. What is the value of n/p ?

- (A) 1 (B) 2 (C) 4 (D) 8 (E) 16

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 17

Not yet answered

Points out of 6

Suppose that $4^a = 5$, $5^b = 6$, $6^c = 7$, and $7^d = 8$. What is $a \cdot b \cdot c \cdot d$?

- (A) 1 (B) $\frac{3}{2}$ (C) 2 (D) $\frac{5}{2}$ (E) 3

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 18

Not yet answered

Points out of 6

All of David's telephone numbers have the form $555 - abc - defg$, where a, b, c, d, e, f , and g are distinct digits and in increasing order, and none is either 0 or 1. How many different telephone numbers can David have?

- (A)1 (B)2 (C)7 (D)8 (E)9

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 19

Not yet answered

Points out of 6

On a certain math exam, 10% of the students got 70 points, 25% got 80 points, 20% got 85 points, 15% got 90 points, and the rest got 95 points. What is the difference between the mean and the median score on this exam?

- (A) 0 (B) 1 (C) 2 (D) 4 (E) 5

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 20

Not yet answered

Points out of 6

What is the average (mean) of all 5-digit numbers that can be formed by using each of the digits 1, 3, 5, 7, and 8 exactly once?

- (A)48000 (B)49999.5 (C)53332.8 (D)55555 (E)56432.8

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 21

Not yet answered

Points out of 6

Forty slips are placed into a hat, each bearing a number 1, 2, 3, 4, 5, 6, 7, 8, 9, or 10, with each number entered on four slips. Four slips are drawn from the hat at random and without replacement. Let p be the probability that all four slips bear the same number. Let q be the probability that two of the slips bear a number a and the other two bear a number $b \neq a$. What is the value of q/p ?

(A)162 (B)180 (C)324 (D)360 (E)720

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 22

Not yet answered

Points out of 6

For how many positive integers n less than or equal to 24 is $n!$ evenly divisible by $1 + 2 + \dots + n$?

(A) 8 (B) 12 (C) 16 (D) 17 (E) 21

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 23

Not yet answered

Points out of 6

In trapezoid $ABCD$ we have \overline{AB} parallel to \overline{DC} , E as the midpoint of \overline{BC} , and F as the midpoint of \overline{DA} . The area of $ABEF$ is twice the area of $FECD$. What is AB/DC ?

(A)2 (B)3 (C)5 (D)6 (E)8

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 24

Not yet answered

Points out of 6

Let x and y be two-digit integers such that y is obtained by reversing the digits of x . The integers x and y satisfy $x^2 - y^2 = m^2$ for some positive integer m . What is $x + y + m$?

(A)88 (B)112 (C)116 (D)144 (E)154

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 25

Not yet answered

Points out of 6

A subset B of the set of integers from 1 to 100, inclusive, has the property that no two elements of B sum to 125. What is the maximum possible number of elements in B ?

(A)50 (B)51 (C)62 (D)65 (E)68

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)