



2009 AMC 10A

For more practice and resources, visit ziml.aretteam.org

The problems in the AMC-Series Contests are copyrighted by American Mathematics Competitions at Mathematical Association of America (www.maa.org).



Question 1

Not yet answered

Points out of 6

One can holds 12 ounces of soda. What is the minimum number of cans needed to provide a gallon (128 ounces) of soda?

(A) 7 (B) 8 (C) 9 (D) 10 (E) 11

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 2

Not yet answered

Points out of 6

Four coins are picked out of a piggy bank that contains a collection of pennies, nickels, dimes, and quarters. Which of the following could *not* be the total value of the four coins, in cents?

(A) 15 (B) 25 (C) 35 (D) 45 (E) 55

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 3

Not yet answered

Points out of 6

Which of the following is equal to $1 + \frac{1}{1 + \frac{1}{1+1}}$?

- (A) $\frac{5}{4}$ (B) $\frac{3}{2}$ (C) $\frac{5}{3}$ (D) 2 (E) 3

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 4

Not yet answered

Points out of 6

Eric plans to compete in a triathlon. He can average 2 miles per hour in the $\frac{1}{4}$ -mile swim and 6 miles per hour in the 3-mile run. His goal is to finish the triathlon in 2 hours. To accomplish his goal what must his average speed in miles per hour, be for the 15-mile bicycle ride?

- (A) $\frac{120}{11}$ (B) 11 (C) $\frac{56}{5}$ (D) $\frac{45}{4}$ (E) 12

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 5

Not yet answered

Points out of 6

What is the sum of the digits of the square of 111, 111, 111?

- (A) 18 (B) 27 (C) 45 (D) 63 (E) 81

Select one:

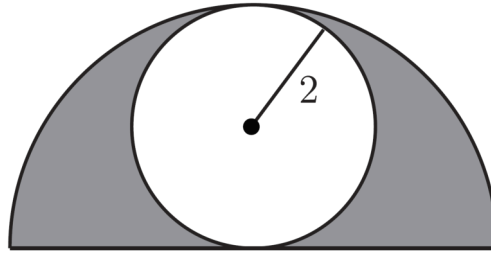
- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 6

Not yet answered

Points out of 6

A circle of radius 2 is inscribed in a semicircle, as shown. The area inside the semicircle but outside the circle is shaded.



What fraction of the semicircle's area is shaded?

- (A) $\frac{1}{2}$ (B) $\frac{\pi}{6}$ (C) $\frac{2}{\pi}$ (D) $\frac{2}{3}$ (E) $\frac{3}{\pi}$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 7

Not yet answered

Points out of 6

A carton contains milk that is 2% fat, an amount that is 40% less fat than the amount contained in a carton of whole milk. What is the percentage of fat in whole milk?

- (A) $\frac{12}{5}$ (B) 3 (C) $\frac{10}{3}$ (D) 38 (E) 42

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 8

Not yet answered

Points out of 6

Three Generations of the Wen family are going to the movies, two from each generation. The two members of the youngest generation receive a 50% discount as children. The two members of the oldest generation receive a 25% discount as senior citizens. The two members of the middle generation receive no discount. Grandfather Wen, whose senior ticket costs \$6.00, is paying for everyone. How many dollars must he pay?

(A) 34 (B) 36 (C) 42 (D) 46 (E) 48

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 9

Not yet answered

Points out of 6

Positive integers a , b , and 2009, with $a < b < 2009$, form a geometric sequence with an integer ratio. What is a ?

(A) 7 (B) 41 (C) 49 (D) 289 (E) 2009

Select one:

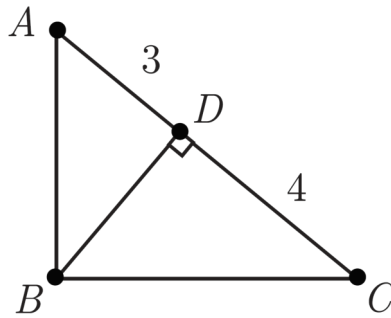
- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 10

Not yet answered

Points out of 6

Triangle ABC has a right angle at B . Point D is the foot of the altitude from B , $AD = 3$, and $DC = 4$.



What is the area of $\triangle ABC$?

- (A) $4\sqrt{3}$ (B) $7\sqrt{3}$ (C) 21 (D) $14\sqrt{3}$ (E) 42

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 11

Not yet answered

Points out of 6

One dimension of a cube is increased by 1, another is decreased by 1, and the third is left unchanged. The volume of the new rectangular solid is 5 less than that of the cube. What was the volume of the cube?

- (A) 8 (B) 27 (C) 64 (D) 125 (E) 216

Select one:

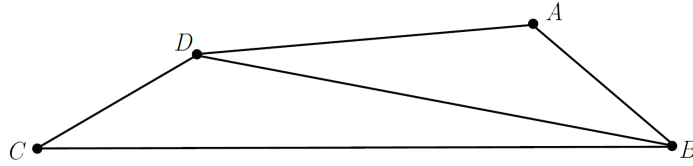
- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 12

Not yet answered

Points out of 6

In quadrilateral $ABCD$, $AB = 5$, $BC = 17$, $CD = 5$, $DA = 9$, and BD is an integer.



What is BD ?

- (A) 11 (B) 12 (C) 13 (D) 14 (E) 15

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 13

Not yet answered

Points out of 6

Suppose that $P = 2^m$ and $Q = 3^n$. Which of the following is equal to 12^{mn} for every pair of integers (m, n) ?

- (A) P^2Q (B) P^nQ^m (C) P^nQ^{2m} (D) $P^{2m}Q^n$ (E) $P^{2n}Q^m$

Select one:

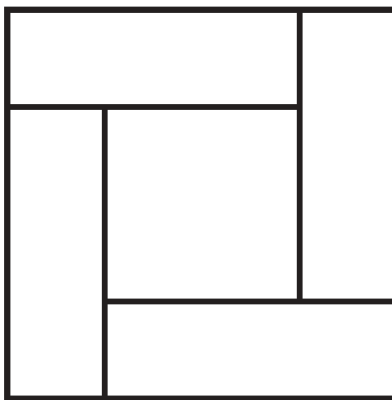
- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 14

Not yet answered

Points out of 6

Four congruent rectangles are placed as shown. The area of the outer square is 4 times that of the inner square.



What is the ratio of the length of the longer side of each rectangle to the length of its shorter side?

- (A) 3 (B) $\sqrt{10}$ (C) $2 + \sqrt{2}$ (D) $2\sqrt{3}$ (E) 4

Select one:

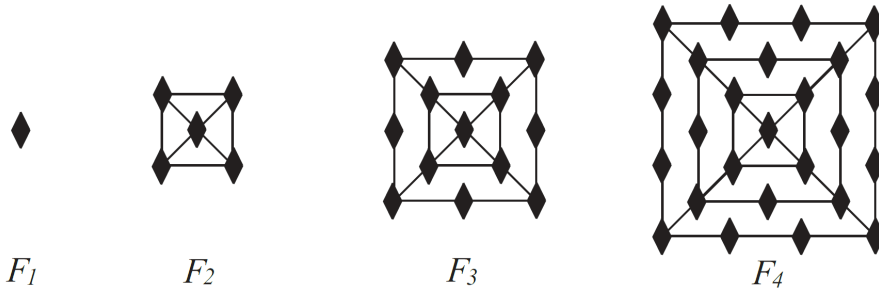
- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 15

Not yet answered

Points out of 6

The figures F_1 , F_2 , F_3 , and F_4 shown are the first in a sequence of figures. For $n \geq 3$, F_n is constructed from F_{n-1} by surrounding it with a square and placing one more diamond on each side of the new square than F_{n-1} had on each side of its outside square. For example, figure F_3 has 13 diamonds.



How many diamonds are there in figure F_{20} ?

- (A) 401 (B) 485 (C) 585 (D) 626 (E) 761

Select one:

- A
 B
 C
 D
 E
 Leave blank (1.5 points)

Question 16

Not yet answered

Points out of 6

Let a , b , c , and d be real numbers with $|a - b| = 2$, $|b - c| = 3$, and $|c - d| = 4$. What is the sum of all possible values of $|a - d|$?

- (A) 9 (B) 12 (C) 15 (D) 18 (E) 24

Select one:

- A
 B
 C
 D
 E
 Leave blank (1.5 points)

Question 17

Not yet answered

Points out of 6

Rectangle $ABCD$ has $AB = 4$ and $BC = 3$. Segment EF is constructed through B so that EF is perpendicular to DB , and A and C lie on DE and DF , respectively. What is EF ?

- (A) 9 (B) 10 (C) $\frac{125}{12}$ (D) $\frac{103}{9}$ (E) 12

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 18

Not yet answered

Points out of 6

At Jefferson Summer Camp, 60% of the children play soccer, 30% of the children swim, and 40% of the soccer players swim. To the nearest whole percent, what percent of the non-swimmers play soccer?

- (A) 30% (B) 40% (C) 49% (D) 51% (E) 70%

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 19

Not yet answered

Points out of 6

Circle A has radius 100. Circle B has an integer radius $r < 100$ and remains internally tangent to circle A as it rolls once around the circumference of circle A . The two circles have the same points of tangency at the beginning and end of circle B 's trip. How many possible values can r have?

- (A) 4 (B) 8 (C) 9 (D) 50 (E) 90

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 20

Not yet answered

Points out of 6

Andrea and Lauren are 20 kilometers apart. They bike toward one another with Andrea traveling three times as fast as Lauren, and the distance between them decreasing at a rate of 1 kilometer per minute. After 5 minutes, Andrea stops biking because of a flat tire and waits for Lauren. After how many minutes from the time they started to bike does Lauren reach Andrea?

- (A) 20 (B) 30 (C) 55 (D) 65 (E) 80

Select one:

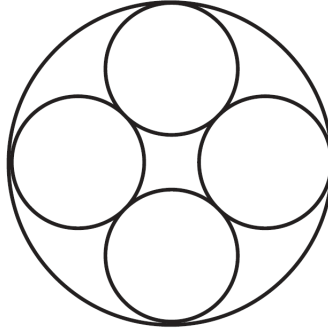
- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 21

Not yet answered

Points out of 6

Many Gothic cathedrals have windows with portions containing a ring of congruent circles that are circumscribed by a larger circle. In the figure shown, the number of smaller circles is four.



What is the ratio of the sum of the areas of the four smaller circles to the area of the larger circle?

- (A) $3 - 2\sqrt{2}$ (B) $2 - \sqrt{2}$ (C) $4(3 - 2\sqrt{2})$ (D) $\frac{1}{2}(3 - \sqrt{2})$ (E) $2\sqrt{2} - 2$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 22

Not yet answered

Points out of 6

Two cubical dice each have removable numbers 1 through 6. The twelve numbers on the two dice are removed, put into a bag, then drawn one at a time and randomly reattached to the faces of the cubes, one number to each face. The dice are then rolled and the numbers on the two top faces are added. What is the probability that the sum is 7?

- (A) $\frac{1}{9}$ (B) $\frac{1}{8}$ (C) $\frac{1}{6}$ (D) $\frac{2}{11}$ (E) $\frac{1}{5}$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 23

Not yet answered

Points out of 6

Convex quadrilateral $ABCD$ has $AB = 9$ and $CD = 12$. Diagonals AC and BD intersect at E , $AC = 14$, and $\triangle AED$ and $\triangle BEC$ have equal areas. What is AE ?

- (A) $\frac{9}{2}$ (B) $\frac{50}{11}$ (C) $\frac{21}{4}$ (D) $\frac{17}{3}$ (E) 6

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 24

Not yet answered

Points out of 6

Three distinct vertices of a cube are chosen at random. What is the probability that the plane determined by these three vertices contains points inside the cube?

- (A) $\frac{1}{4}$ (B) $\frac{3}{8}$ (C) $\frac{4}{7}$ (D) $\frac{5}{7}$ (E) $\frac{3}{4}$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 25

Not yet answered

Points out of 6

For $k > 0$, let $I_k = 10 \dots 064$, where there are k zeros between the 1 and the 6. Let $N(k)$ be the number of factors of 2 in the prime factorization of I_k . What is the maximum value of $N(k)$?

- (A) 6 (B) 7 (C) 8 (D) 9 (E) 10

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

