

2017 AMC 10A

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Not yet answered

Points out of 6

What is the value of (2(2(2(2(2+1)+1)+1)+1)+1)+1)?

- **(A)** 70
- **(B)** 97
- (C) 127 (D) 159 (E) 729

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 2

Not yet answered

Points out of 6

Pablo buys popsicles for his friends. The store sells single popsicles for \$1 each, 3-popsicle boxes for \$2 each, and 5-popsicle boxes for \$3. What is the greatest number of popsicles that Pablo can buy with \$8?

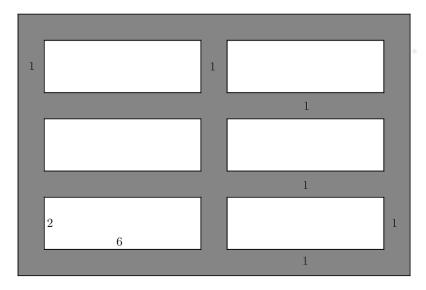
- **(A)** 8
- **(B)** 11
- **(C)** 12
- **(D)** 13
- **(E)** 15

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Not yet answered

Points out of 6

Tamara has three rows of two 6-feet by 2-feet flower beds in her garden. The beds are separated and also surrounded by 1-foot-wide walkways, as shown on the diagram.



What is the total area of the walkways, in square feet?

- **(A)** 72
- **(B)** 78
- **(C)** 90
- **(D)** 120
- **(E)** 150

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 4

Not yet answered

Points out of 6

Mia is helping her mom pick up 30 toys that are strewn on the floor. Mia's mom manages to put 3 toys into the toy box every 30 seconds, but each time immediately after those 30 seconds have elapsed, Mia takes 2 toys out of the box. How much time, in minutes, will it take Mia and her mom to put all 30 toys into the box for the first time?

- **(A)** 13.5
- **(B)** 14
- (C) 14.5
- **(D)** 15
- (E) 15.5

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 5	The sum of two nonzero real numbers is 4 times their product. What is the sum of the reciprocals of the two numbers?												
Not yet answered Points out of 6	(A) 1 (B) 2 (C) 4 (D) 8 (E) 12												
	Select one: • A												
									B C D E Leave blank (1.5 points)				
6													
Question 6 Not yet answered		•	•	•	ne multiple choice questions right on the upcoming these statements necessarily follows logically?	j exam							
Points out of 6	(A) If Lewis did not receive an A, then he got all of the multiple choice questions wrong.												
	(B) If Lewis did not receive an A, then he got at least one of the multiple choice questions wrong.(C) If Lewis got at least one of the multiple choice questions wrong, then he did not receive an A.												
	` ′	_			all of the multiple choice questions right.	t receive an A.							
	(E) If Lewis received an A, then he got at least one of the multiple choice questions right. Select one:												
	○ A												
	○ B												
	○ c												
	□ D□ E												
								○ Leave blank (1.5 points)					
	Question 7	Jerry and	Silvia wante	ed to go from	the southw	est corner of a square field to the northeast corner	Jerry						
Not yet answered	Jerry and Silvia wanted to go from the southwest corner of a square field to the northeast corner. Jerry walked due east and then due north to reach the goal, but Silvia headed northeast and reached the goal												
Points out of 6	_	a straight lir I to Jerry's tr		f the followin	g is closest to how much shorter Silvia's trip was,								
	(A) 30%	(B)	40% (0	C) 50%	(D) 60% (E) 70%								
	Select on	e:											
	○ A												
	○ B												
	○ C												
	O D												
	○ E												
	○ Leav	e blank (1.5	points)										

Question 8 Not yet answered Points out of 6	At a gathering of 30 people, there are 20 people who all know each other and 10 people who know no one. People who know each other a hug, and people who do not know each other shake hands. How many handshakes occur?							
Points out of 6	(A) 240 (B) 245 (C) 290 (D) 480 (E) 490 Select one: A B C C D Leave blank (1.5 points)							
Question 9 Not yet answered Points out of 6	Minnie rides on a flat road at 20 kilometers per hour (kph), downhill at 30 kph, and uphill at 5 kph. Penny rides on a flat road at 30 kph, downhill at 40 kph, and uphill at 10 kph. Minnie goes from town A to town B , a distance of 10 km all uphill, then from town B to town C , a distance of 15 km all downhill, and then back to town A , a distance of 20 km on the flat. Penny goes the other way around using the same route. How many more minutes does it take Minnie to complete the 45 -km ride than it takes Penny? (A) 45 (B) 60 (C) 65 (D) 90 (E) 95 Select one: A B C D Leave blank (1.5 points)							
Question 10 Not yet answered Points out of 6	Joy has 30 thin rods, one each of every integer length from 1 cm through 30 cm. She places the rods with lengths 3 cm, 7 cm, and 15 cm on a table. She then wants to choose a fourth rod that she can put with these three to form a quadrilateral with positive area. How many of the remaining rods can she choose as the fourth rod? (A) 16 (B) 17 (C) 18 (D) 19 (E) 20 Select one: A B C D E Leave blank (1.5 points)							

Not yet answered

Points out of 6

The region consisting of all point in three-dimensional space within 3 units of line segment AB has volume 216 π . What is the length AB?

(A) 6

(B) 12

(C) 18

(D) 20

(E) 24

Select one:

- A
- B

- Leave blank (1.5 points)

Question 12

Not yet answered

Points out of 6

Let S be a set of points (x, y) in the coordinate plane such that two of the three quantities 3, x + 2, and y-4 are equal and the third of the three quantities is no greater than this common value. Which of the following is a correct description for S?

- (A) a single point
- (B) two intersecting lines
- (C) three lines whose pairwise intersections are three distinct points
- (**D**) a triangle
- (E) three rays with a common endpoint

Select one:

- A
- B

- E
- Leave blank (1.5 points)

Question 13

Not yet answered

Points out of 6

Define a sequence recursively by $F_0=0,\; F_1=1,$ and $F_n=$ the remainder when $F_{n-1}+F_{n-2}$ is divided by 3, for all $n \geq 2$. Thus the sequence starts $0,1,1,2,0,2,\ldots$ What is $F_{2017} + F_{2018} + F_{2019} + F_{2020} + F_{2021} + F_{2022} + F_{2023} + F_{2024}?$

(A) 6

- **(B)** 7 **(C)** 8 **(D)** 9 **(E)** 10

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Not yet answered

Points out of 6

Every week Roger pays for a movie ticket and a soda out of his allowance. Last week, Roger's allowance was A dollars. The cost of his movie ticket was 20% of the difference between A and the cost of his soda, while the cost of his soda was 5% of the difference between A and the cost of his movie ticket. To the nearest whole percent, what fraction of A did Roger pay for his movie ticket and soda?

- (A) 9%
- **(B)** 19%
- (C) 22%
- **(D)** 23%
- **(E)** 25%

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 15

Not yet answered

Points out of 6

Chloé chooses a real number uniformly at random from the interval [0, 2017]. Independently, Laurent chooses a real number uniformly at random from the interval [0,4034]. What is the probability that Laurent's number is greater than Chloé's number?

- **(A)** $\frac{1}{2}$

- (B) $\frac{2}{3}$ (C) $\frac{3}{4}$ (D) $\frac{5}{6}$ (E) $\frac{7}{8}$

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Not yet answered

Points out of 6

There are 10 horses, named Horse 1, Horse $2, \ldots$, Horse 10. They get their names from how many minutes it takes them to run one lap around a circular race track: Horse k runs one lap in exactly kminutes. At time 0 all the horses are together at the starting point on the track. The horses start running in the same direction, and they keep running around the circular track at their constant speeds. The least time S>0, in minutes, at which all 10 horses will again simultaneously be at the starting point is S=2520. Let T>0 be the least time, in minutes, such that at least 5 of the horses are again at the starting point. What is the sum of the digits of T?

- (A) 2
- **(B)** 3
- (C) 4 (D) 5
- (\mathbf{E}) 6

Select one:

- A
- B
- С
- D
- E
- Leave blank (1.5 points)

Question 17

Not yet answered

Points out of 6

Distinct points $P,\,Q,\,R,\,S$ lie on the circle $x^2+y^2=25$ and have integer coordinates. The distances PQ and RS are irrational numbers. What is the greatest possible value of the ratio $\frac{PQ}{RS}$?

- **(A)** 3

- **(B)** 5 **(C)** $3\sqrt{5}$ **(D)** 7 **(E)** $5\sqrt{2}$

- A
- В
- D
- Ε
- Leave blank (1.5 points)

Question 18 Not yet answered Points out of 6	Amelia has a coin that lands heads with probability $\frac{1}{3}$, and Blaine has a coin that lands on heads with probability $\frac{2}{5}$. Amelia and Blaine alternately toss their coins until someone gets a head; the first one to get a head wins. All coin tosses are independent. Amelia goes first. The probability that Amelia wins is $\frac{p}{q}$, where p and q are relatively prime positive integers. What is $q-p$? (A) 1 (B) 2 (C) 3 (D) 4 (E) 5 Select one: A B C D E Leave blank (1.5 points)
Question 19 Not yet answered Points out of 6	Alice refuses to sit next to either Bob or Carla. Derek refuses to sit next to Eric. How many ways are there for the five of them to sit in a row of 5 chairs under these conditions? (A) 12 (B) 16 (C) 28 (D) 32 (E) 40 Select one: A B C D Leave blank (1.5 points)
Question 20 Not yet answered Points out of 6	Let $S(n)$ equal the sum of the digits of positive integer n . For example, $S(1507)=13$. For a particular positive integer n , $S(n)=1274$. Which of the following could be the value of $S(n+1)$? (A) 1 (B) 3 (C) 12 (D) 1239 (E) 1265 Select one: A B C C D Leave blank (1.5 points)

Not yet answered

Points out of 6

A square with side length x is inscribed in a right triangle with sides of length 3, 4, and 5 so that one vertex of the square coincides with the right-angle vertex of the triangle. A square with side length y is inscribed in another right triangle with sides of length 3, 4, and 5 so that one side of the square lies on the hypotenuse of the triangle. What is $\frac{x}{}$?

(A)
$$\frac{12}{13}$$

(B)
$$\frac{35}{37}$$

(A)
$$\frac{12}{13}$$
 (B) $\frac{35}{37}$ (C) 1 (D) $\frac{37}{35}$ (E) $\frac{13}{12}$

(E)
$$\frac{13}{12}$$

Select one:

- A

- D
- \bigcirc E
- Leave blank (1.5 points)

Question 22

Not yet answered

Points out of 6

Sides AB and AC of equilateral triangle ABC are tangent to a circle at points B and C respectively. What fraction of the area of $\triangle ABC$ lies outside the circle?

(A)
$$\frac{4\sqrt{3}\pi}{27} - \frac{1}{3}$$

(B)
$$\frac{\sqrt{3}}{2} - \frac{\pi}{8}$$

(C)
$$\frac{1}{2}$$

(A)
$$\frac{4\sqrt{3}\pi}{27} - \frac{1}{3}$$
 (B) $\frac{\sqrt{3}}{2} - \frac{\pi}{8}$ (C) $\frac{1}{2}$ (D) $\sqrt{3} - \frac{2\sqrt{3}\pi}{9}$ (E) $\frac{4}{3} - \frac{4\sqrt{3}\pi}{27}$

(E)
$$\frac{4}{3} - \frac{4\sqrt{3}\pi}{27}$$

Select one:

- A
- C
- E
- Leave blank (1.5 points)

Question 23

Not yet answered

Points out of 6

How many triangles with positive area have all their vertices at points $\left(i,j\right)$ in the coordinate plane, where i and j are integers between 1 and 5, inclusive?

- **(A)** 2128
- **(B)** 2148
- **(C)** 2160
- **(D)** 2200
- **(E)** 2300

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Not yet answered

Points out of 6

For certain real numbers a, b, and c, the polynomial

$$g(x) = x^3 + ax^2 + x + 10$$

has three distinct roots, and each root of g(x) is also a root of the polynomial

$$f(x) = x^4 + x^3 + bx^2 + 100x + c.$$

What is f(1)?

$$(A) - 9009$$

$$(A) - 9009$$
 $(B) - 8008$ $(C) - 7007$ $(D) - 6006$ $(E) - 5005$

(C)
$$-7007$$

(D)
$$-6006$$

(E)
$$-5005$$

Select one:

- A
- B
- C
- D
- E
- Leave blank (1.5 points)

Question 25

Not yet answered

Points out of 6

How many integers between 100 and 999, inclusive, have the property that some permutation of its digits is a multiple of 11 between 100 and 999? For example, both 121 and 211 have this property.

- (A) 226
- **(B)** 243
- **(C)** 270
- **(D)** 469
- **(E)** 486

- A
- B
- C
- D
- E
- Leave blank (1.5 points)