2025 AMC 10A

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Question 1

Not yet answered

Points out of 6

Andy and Betsy both live in Mathville. Andy leaves Mathville on his bicycle at $1:30$, traveling due north at a steady 8 miles per hour. Betsy leaves on her bicycle from the same point at $2:30$, traveling due east at a steady 12 miles per hour. At what time will they be exactly the same distance from their common starting point?

$\textbf{(A)}\ 3{:}30 \qquad \textbf{(B)}\ 3{:}45 \qquad \textbf{(C)}\ 4{:}00 \qquad \textbf{(D)}\ 4{:}15 \qquad \textbf{(E)}\ 4{:}30$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 2

Not yet answered

Points out of 6

A box contains 10 pounds of a nut mix that is 50 percent peanuts, 20 percent cashews, and 30 percent almonds. A second nut mix containing 20 percent peanuts, 40 percent cashews, and 40 percent almonds is added to the box resulting in a new nut mix that is 40 percent peanuts. How many pounds of cashews are now in the box?

$\textbf{(A)}\ 3.5 \qquad \textbf{(B)}\ 4 \qquad \textbf{(C)}\ 4.5 \qquad \textbf{(D)}\ 5 \qquad \textbf{(E)}\ 6$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 3

Not yet answered

Points out of 6

How many isosceles triangles are there with positive area whose side lengths are all positive integers and whose longest side has length 2025?

$\textbf{(A)}\ 2025 \qquad \textbf{(B)}\ 2026 \qquad \textbf{(C)}\ 3012 \qquad \textbf{(D)}\ 3037 \qquad \textbf{(E)}\ 4050$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 4

Not yet answered

Points out of 6

A team of students is going to compete against a team of teachers in a trivia contest. The total number of students and teachers is 15. Ash, a cousin of one of the students, wants to join the contest. If Ash plays with the students, the average age on that team will increase from 12 to 14. If Ash plays with the teachers, the average age on that team will decrease from 55 to 52. How old is Ash?

$\textbf{(A)}\ 28 \qquad \textbf{(B)}\ 29 \qquad \textbf{(C)}\ 30 \qquad \textbf{(D)}\ 32 \qquad \textbf{(E)}\ 33$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 5

Not yet answered

Points out of 6

Consider the sequence of positive integers

$$1, 2, 1, 2, 3, 2, 1, 2, 3, 4, 3, 2, 1, 2, 3, 4, 5, 4, 3, 2, 1, 2, 3, 4, 5, 6, 5, 4, 3, 2, 1, 2 \ldots$$

What is the 2025th term in the sequence?

$\textbf{(A)}\ 5 \qquad \textbf{(B)}\ 15 \qquad \textbf{(C)}\ 16 \qquad \textbf{(D)}\ 44 \qquad \textbf{(E)}\ 45$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 6

Not yet answered

Points out of 6

In an equilateral triangle each interior angle is trisected by a pair of rays. The intersection of the interiors of the middle 20°-angle at each vertex is the interior of a convex hexagon. What is the degree measure of the smallest angle of this hexagon?

$\textbf{(A)}\ 80 \qquad \textbf{(B)}\ 90 \qquad \textbf{(C)}\ 100 \qquad \textbf{(D)}\ 110 \qquad \textbf{(E)}\ 120$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 7

Not yet answered

Points out of 6

Suppose a and b are real numbers. When the polynomial $x^3 + x^2 + ax + b$ is divided by $x - 1$, the remainder is 4. When the polynomial is divided by $x - 2$, the remainder is 6. What is $b - a$?

$\textbf{(A)}\ 14 \qquad \textbf{(B)}\ 15 \qquad \textbf{(C)}\ 16 \qquad \textbf{(D)}\ 17 \qquad \textbf{(E)}\ 18$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 8

Not yet answered

Points out of 6

Agnes writes the following four statements on a blank piece of paper.

- At least one of these statements is true.
- At least two of these statements are true.
- At least two of these statements are false.
- At least one of these statements is false.

Each statement is either true or false. How many false statements did Agnes write on the paper?

$\textbf{(A)}\ 0 \qquad \textbf{(B)}\ 1 \qquad \textbf{(C)}\ 2 \qquad \textbf{(D)}\ 3 \qquad \textbf{(E)}\ 4$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 9

Not yet answered

Points out of 6

Let $f(x) = 100x^3 - 300x^2 + 200x$. For how many real numbers a does the graph of $y = f(x - a)$ pass through the point $(1, 25)$?

(A) 1 **(B)** 2 **(C)** 3 **(D)** 4 **(E)** more than 4

Select one:

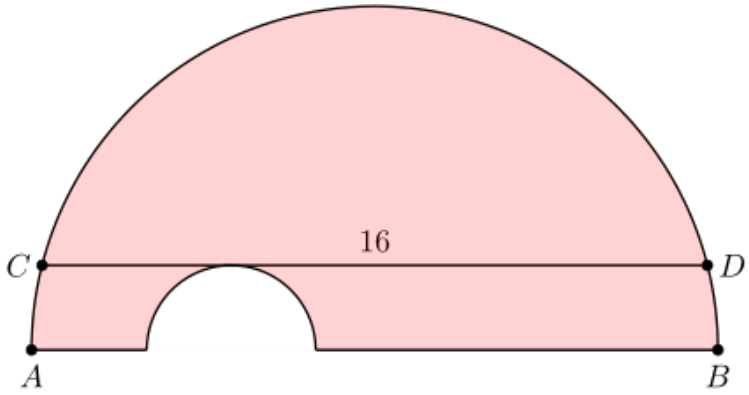
- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 10

Not yet answered

Points out of 6

A semicircle has diameter $\overline{AB}$ and chord $\overline{CD}$ of length 16 parallel to $\overline{AB}$. A smaller semicircle with diameter on $\overline{AB}$ and tangent to $\overline{CD}$ is cut from the larger semicircle, as shown below.



What is the area of the resulting figure, shown shaded?

(A) 16π **(B)** 24π **(C)** 32π **(D)** 48π **(E)** 64π

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 11

Not yet answered

Points out of 6

The sequence $1, x, y, z$ is arithmetic. The sequence $1, p, q, z$ is geometric. Both sequences are strictly increasing and contain only integers, and z is as small as possible. What is the value of $x + y + z + p + q$?

$\textbf{(A)}\ 66 \qquad \textbf{(B)}\ 91 \qquad \textbf{(C)}\ 103 \qquad \textbf{(D)}\ 132 \qquad \textbf{(E)}\ 149$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 12

Not yet answered

Points out of 6

Carlos uses a 4-digit passcode to unlock his computer. In his passcode, exactly one digit is even, exactly one (possibly different) digit is prime, and no digit is 0. How many 4-digit passcodes satisfy these conditions?

$\textbf{(A)}\ 176 \qquad \textbf{(B)}\ 192 \qquad \textbf{(C)}\ 432 \qquad \textbf{(D)}\ 464 \qquad \textbf{(E)}\ 608$

Select one:

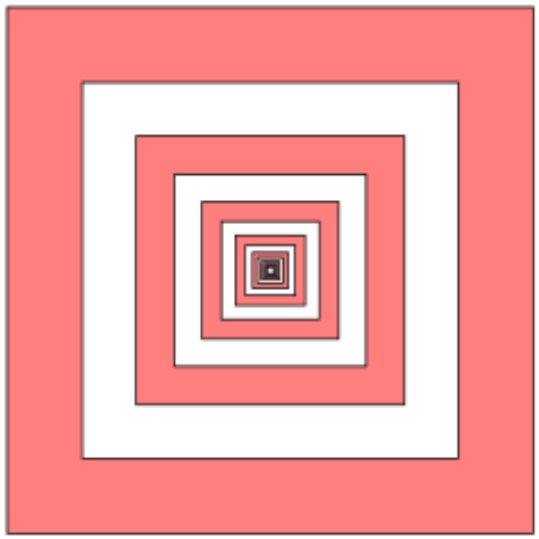
- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 13

Not yet answered

Points out of 6

In the figure below, the outside square contains infinitely many squares, each of them with the same center and sides parallel to the outside square. The ratio of the side length of a square to the side length of the next inner square is k, where $0 < k < 1$. The spaces between squares are alternately shaded, as shown in the figure (which is not necessarily drawn to scale).



The area of the shaded portion of the figure is 64% of the area of the original square. What is k?

$\textbf{(A)}\ \frac{3}{5} \qquad \textbf{(B)}\ \frac{16}{25} \qquad \textbf{(C)}\ \frac{2}{3} \qquad \textbf{(D)}\ \frac{3}{4} \qquad \textbf{(E)}\ \frac{4}{5}$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 14

Not yet answered

Points out of 6

Six chairs are arranged around a round table. Two students and two teachers randomly select four of the chairs to sit in. What is the probability that the two students will sit in two adjacent chairs and the two teachers will also sit in two adjacent chairs?

(A) $\frac{1}{6}$ **(B)** $\frac{1}{5}$ **(C)** $\frac{2}{9}$ **(D)** $\frac{3}{13}$ **(E)** $\frac{1}{4}$

Select one:

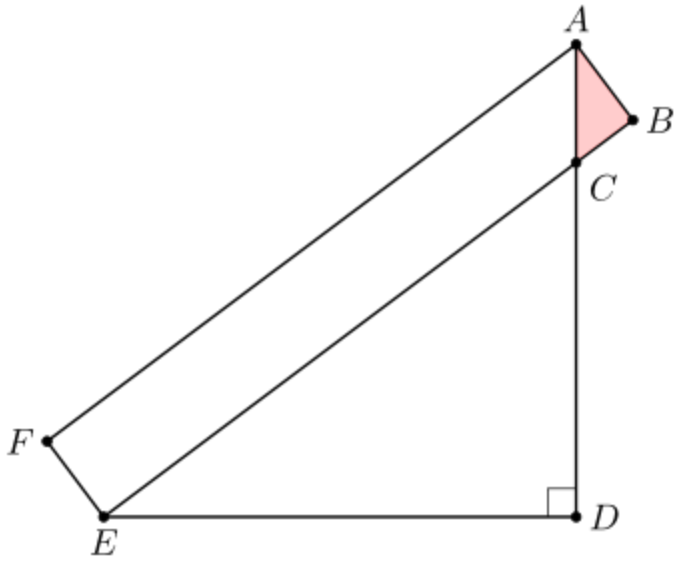
- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 15

Not yet answered

Points out of 6

In the figure below, $ABEF$ is a rectangle, $\overline{AD} \perp \overline{DE}$, $AF = 7$, $AB = 1$, and $AD = 5$.



What is the area of $\triangle ABC$?

(A) $\frac{3}{8}$ **(B)** $\frac{4}{9}$ **(C)** $\frac{1}{8}\sqrt{13}$ **(D)** $\frac{7}{15}$ **(E)** $\frac{1}{8}\sqrt{15}$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 16

Not yet answered

Points out of 6

There are three jars. Each of three coins is placed in one of the three jars, chosen at random and independently of the placement of the other coins. What is the expected number of coins in a jar with the most coins?

$\textbf{(A)}\ \frac{4}{3}$ $\textbf{(B)}\ \frac{13}{9}$ $\textbf{(C)}\ \frac{5}{8}$ $\textbf{(D)}\ \frac{17}{9}$ $\textbf{(E)}\ 2$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 17

Not yet answered

Points out of 6

Let N be the unique positive integer such that dividing 273436 by N leaves a remainder of 16 and dividing 272760 by N leaves a remainder of 15. What is the tens digit of N?

$\textbf{(A)}\ 0$ $\textbf{(B)}\ 1$ $\textbf{(C)}\ 2$ $\textbf{(D)}\ 3$ $\textbf{(E)}\ 4$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 18

Not yet answered

Points out of 6

The *harmonic mean* of a collection of numbers is the reciprocal of the arithmetic mean of the reciprocals of the numbers in the collection. For example, the harmonic mean of 4, 4 and 5 is

$$\frac{1}{\frac{1}{3}(\frac{1}{4}+\frac{1}{4}+\frac{1}{5})}=\frac{30}{7}.$$

What is the harmonic mean of all the real roots of the 4050th degree polynomial

$$\prod_{k=1}^{2025}(kx^2-4x-3)=(x^2-4x-3)(2x^2-4x-3)(3x^2-4x-3)\ldots(2025x^2-4x-3)?$$

$\textbf{(A)}\ -\frac{5}{3}\qquad\textbf{(B)}\ -\frac{3}{2}\qquad\textbf{(C)}\ -\frac{6}{5}\qquad\textbf{(D)}\ -\frac{5}{6}\qquad\textbf{(E)}\ -\frac{2}{3}$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 19

Not yet answered

Points out of 6

An array of numbers is constructed beginning with the numbers -1, 3, and 1 in the top row. Each adjacent pair of numbers is summed to produce a number in the next row. Each row begins and ends with -1 and 1, respectively.

$$\begin{array}{ccccccc} & & -1 & & 3 & & 1 \\ & -1 & & 2 & & 4 & & 1 \\ -1 & & 1 & & 6 & & 5 & & 1 \end{array}$$

If the process continues, one of the rows will sum to $12{,}288$. In that row, what is the third number from the left?

$\textbf{(A)}\ -29\qquad\textbf{(B)}\ -21\qquad\textbf{(C)}\ -14\qquad\textbf{(D)}\ -18\qquad\textbf{(E)}\ -3$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 20

Not yet answered

Points out of 6

A silo (right circular cylinder) with diameter 20 meters stands in a field. MacDonald is located 20 meters west and 15 meters south of the center of the silo. McGregor is located 20 meters east and $g > 0$ meters south of the center of the silo. The line of sight between MacDonald and McGregor is tangent to the silo. The value of g can be written as $\frac{a\sqrt{b}-c}{d}$, where $a, b, c,$ and d are positive integers, b is not divisible by the square of any prime, and d is relatively prime to the greatest common divisor of a and c. What is $a+b+c+d$?

$\mathbf{(A)}\ 119 \qquad \mathbf{(B)}\ 120 \qquad \mathbf{(C)}\ 121 \qquad \mathbf{(D)}\ 122 \qquad \mathbf{(E)}\ 123$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 21

Not yet answered

Points out of 6

A set of numbers is called *sum-free* if whenever x and y are (not necessarily distinct) elements of the set, $x+y$ is not an element of the set. For example, $\{1,4,6\}$ and the empty set are sum-free, but $\{1,4,5\}$ is not. What is the greatest possible number of elements in a sum-free subset of $\{1,2,3,\ldots,20\}$?

$\mathbf{(A)}\ 8 \qquad \mathbf{(B)}\ 9 \qquad \mathbf{(C)}\ 10 \qquad \mathbf{(D)}\ 11 \qquad \mathbf{(E)}\ 12$

Select one:

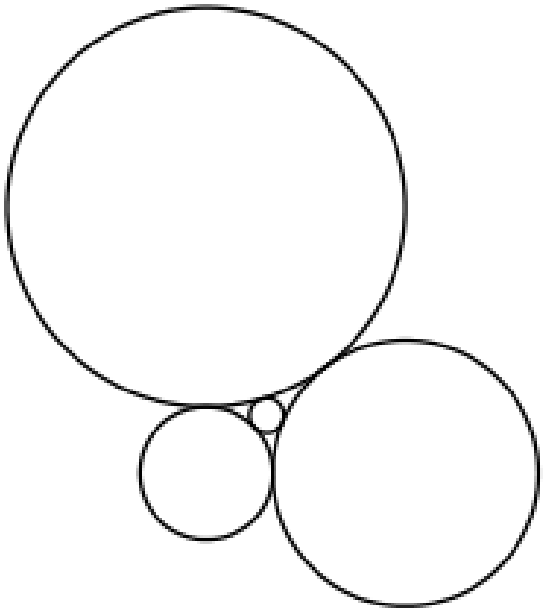
- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 22

Not yet answered

Points out of 6

A circle of radius r is surrounded by three circles, whose radii are 1, 2, and 3, all externally tangent to the inner circle and externally tangent to each other, as shown in the diagram below.



What is r?

$\textbf{(A)}\ \frac{1}{4}$ $\textbf{(B)}\ \frac{6}{23}$ $\textbf{(C)}\ \frac{3}{11}$ $\textbf{(D)}\ \frac{5}{17}$ $\textbf{(E)}\ \frac{3}{10}$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 23

Not yet answered

Points out of 6

Triangle $\triangle ABC$ has side lengths $AB = 80$, $BC = 45$, and $AC = 75$. The bisector of $\angle B$ and the altitude to side $\overline{AB}$ intersect at point P. What is BP?

$\textbf{(A)}\ 18$ $\textbf{(B)}\ 19$ $\textbf{(C)}\ 20$ $\textbf{(D)}\ 21$ $\textbf{(E)}\ 22$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 24

Not yet answered

Points out of 6

Call a positive integer fair if no digit is used more than once, it has no 0s, and no digit is adjacent to two greater digits. For example, $196, 23$ and 12463 are fair, but $1546, 320$, and 34321 are not. How many fair positive integers are there?

$\textbf{(A)}\ 511 \qquad \textbf{(B)}\ 2584 \qquad \textbf{(C)}\ 9841 \qquad \textbf{(D)}\ 17711 \qquad \textbf{(E)}\ 19682$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 25

Not yet answered

Points out of 6

A point P is chosen at random inside square $ABCD$. The probability that $\overline{AP}$ is neither the shortest nor the longest side of $\triangle APB$ can be written as $\frac{a+b\pi-c\sqrt{d}}{e}$, where a, b, c, d, and e are positive integers, $\gcd(a, b, c, e) = 1$, and d is not divisible by the square of a prime. What is $a + b + c + d + e$?

$\textbf{(A)}\ 25 \qquad \textbf{(B)}\ 26 \qquad \textbf{(C)}\ 27 \qquad \textbf{(D)}\ 28 \qquad \textbf{(E)}29$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**