

2023 AMC 12A

Try this exam as a timed Mock Exam on the ZIML Practice Page (click here)

View answers and concepts tested in our 2023 AMC 10A+12A Blog Post (click here)

The problems in the AMC-Series Contests are copyrighted by American Mathematics Competitions at Mathematical Association of America (www.maa.org).



Not yet answered

Points out of 6

Cities A and B are 45 miles apart. Alicia lives in A and Beth lives in B. Alicia bikes towards B at 18 miles per hour. Leaving at the same time, Beth bikes toward A at 12 miles per hour. How many miles from City A will they be when they meet?

- **(A)** 20
- **(B)** 24 **(C)** 25 **(D)** 26
- (E) 27

Select one:

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \bigcirc E
- Control Leave blank (1.5 points)

Question 2

Not yet answered

Points out of 6

The weight of $\frac{1}{3}$ of a large pizza together with $3\frac{1}{2}$ cups of orange slices is the same as the weight of $\frac{3}{4}$ of a large pizza together with $\frac{1}{2}$ cup of orange slices. A cup of orange slices weighs $\frac{1}{4}$ of a pound. What is the weight, in pounds, of a large pizza?

- (A) $1\frac{4}{5}$ (B) 2 (C) $2\frac{2}{5}$ (D) 3 (E) $3\frac{3}{5}$

- \bigcirc A
- \bigcirc B

- Leave blank (1.5 points)

Not yet answered

Points out of 6

How many positive perfect squares less than 2023 are divisible by 5?

- **(A)** 8
- **(B)** 9
- **(C)** 10
- **(D)** 11
- **(E)** 12

Select one:

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \bigcirc E
- Leave blank (1.5 points)

Question 4

Not yet answered

Points out of 6

How many digits are in the base-ten representation of $8^5 \cdot 5^{10} \cdot 15^5$?

- **(A)** 14
- **(B)** 15
- **(C)** 16
- **(D)** 17
- **(E)** 18

Select one:

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \bigcirc E
- Leave blank (1.5 points)

Question 5

Not yet answered

Points out of 6

Janet rolls a standard 6-sided die 4 times and keeps a running total of the numbers she rolls. What is the probability that at some point, her running total will equal 3?

- (A) $\frac{2}{9}$ (B) $\frac{49}{216}$ (C) $\frac{25}{108}$ (D) $\frac{17}{72}$ (E) $\frac{13}{54}$

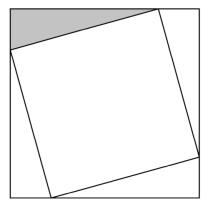
- \bigcirc A
- \bigcirc B
- C
- \bigcirc D
- \cap E
- Leave blank (1.5 points)

Question 6 Not yet answered	Points A and B lie on the graph of $y=\log_2 x$. The midpoint of \overline{AB} is $(6,2)$. What is the positive difference between the x -coordinates of A and B ?					
Points out of 6				(D) $4\sqrt{5}$		
	Select one: A B C D E Leave bla	ank (1.5 points)			
Question 7 Not yet answered Points out of 6	followed by a 2 Day this year is an even numb (A) 5 (If Select one: A B C D E	2-digit month, for significations of the signification of the significat	ollowed by a 20230428. Fine 8-digital differential differ	2-digit date with for how many d splay for that da	per consisting of a 4-digit year, nin the month. For example, Arbor ates in 2023 will each digit appear ate?	
Question 8 Not yet answered Points out of 6	an 11 on the rithree quizzes, (A) 4 (If Select one: A B C D E	next quiz, her m her mean will i	ean will incrence by 2	ease by 1. If she	this semester. If Maureen scores e scores an 11 on each of the next ean of her quiz scores currently?	

Not yet answered

Points out of 6

A square of area 2 is inscribed in a square of area 3, creating four congruent triangles, as shown below. What is the ratio of the shorter leg to the longer leg in the shaded right triangle?



- **(A)** $\frac{1}{5}$ **(B)** $\frac{1}{4}$ **(C)** $2-\sqrt{3}$
- **(D)** $\sqrt{3} \sqrt{2}$ **(E)** $\sqrt{2} 1$

Select one:

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \bigcirc E
- Leave blank (1.5 points)

Question 10

Not yet answered

Points out of 6

Positive real numbers x and y satisfy $y^3=x^2$ and $(y-x)^2=4y^2$. What is x+y?

- **(A)** 12
- **(B)** 18 **(C)** 24 **(D)** 36 **(E)** 42

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \bigcirc E
- Leave blank (1.5 points)

Not yet answered

Points out of 6

What is the degree measure of the acute angle formed by lines with slopes 2 and $\frac{1}{3}$?

(A) 30

(B) 37.5

(C) 45

(D) 52.5

(E) 60

Select one:

 \bigcirc A

 \bigcirc B

 \bigcirc C

 \bigcirc D

 \bigcirc E

○ Leave blank (1.5 points)

Question 12

Not yet answered

Points out of 6

What is the value of

$$2^3 - 1^3 + 4^3 - 3^3 + 6^3 - 5^3 + \dots + 18^3 - 17^3$$
?

(A) 2023

(B) 2679 **(C)** 2941 **(D)** 3159 **(E)** 3235

Select one:

 \bigcirc A

 \bigcirc B

 \bigcirc C

 \bigcirc D

 \bigcirc E

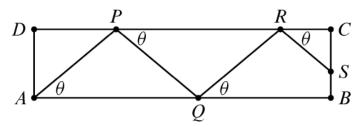
Leave blank (1.5 points)

Question 13 Not yet answered Points out of 6	In a table tennis tournament every participant played every other participant exactly once. Although there were twice as many right-handed players as left-handed players, the number of games won by left-handed players was 40% more than the number of games won by right-handed players. (There were no ties and no ambidextrous players.) What is the total number of games played?					
	(A) 15 (B) 36 (C) 45 (D) 48 (E) 66					
	Select one: A B C D E Leave blank (1.5 points)					
Question 14 Not yet answered	How many complex numbers satisfy the equation $z^5=\overline{z}$, where \overline{z} is the conjugate of the complex number z ?					
Points out of 6	(A) 2 (B) 3 (C) 5 (D) 6 (E) 7					
	Select one: A B C D E Leave blank (1.5 points)					

Not yet answered

Points out of 6

Usain is walking for exercise by zigzagging across a 100-meter by 30-meter rectangular field, beginning at point A and ending on the segment \overline{BC} . He wants to increase the distance walked by zigzagging as shown in the figure below (APQRS). What angle θ $\angle PAB = \angle QPC = \angle RQB = \cdots$ will produce in a length that is 120 meters? (This figure is not drawn to scale. Do not assume that he zigzag path has exactly four segments as shown; there could be more or fewer.)



- (A) $\arccos \frac{5}{6}$ (B) $\arccos \frac{4}{5}$ (C) $\arccos \frac{3}{10}$
- **(D)** $\arcsin \frac{4}{5}$ **(E)** $\arcsin \frac{5}{6}$

Select one:

- \bigcirc A

- \bigcirc D
- \cap E
- Leave blank (1.5 points)

Question 16

Not yet answered

Points out of 6

Consider the set of complex numbers z satisfying $|1+z+z^2|=4$. The maximum value of the imaginary part of z can be written in the form $\frac{\sqrt{m}}{n}$, where m and n are relatively prime positive integers. What is m + n?

- **(A)** 20
- **(B)** 21
- (C) 22
- **(D)** 23
- (E) 24

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \cap E
- Leave blank (1.5 points)

Not yet answered

Points out of 6

Flora the frog starts at 0 on the number line and makes a sequence of jumps to the right. In any one jump, independent of previous jumps, Flora leaps a positive integer distance mwith probability $\frac{1}{2^m}$.

What is the probability that Flora will eventually land at 10?

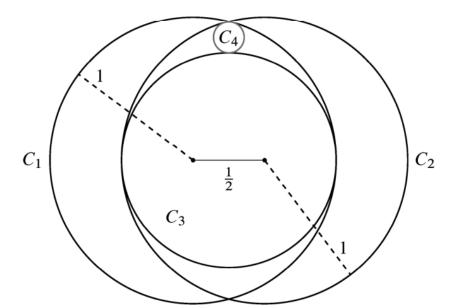
- **(A)** $\frac{5}{512}$
- (B) $\frac{45}{1024}$ (C) $\frac{127}{1024}$ (D) $\frac{511}{1024}$ (E) $\frac{1}{2}$

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \bigcirc E
- Leave blank (1.5 points)

Not yet answered

Points out of 6

Circle C_1 and C_2 each have radius 1, and the distance between their centers is $\frac{1}{2}$. Circle C_3 is the largest circle internally tangent to both C_1 and C_2 . Circle C_4 is internally tangent to both C_1 and C_2 and externally tangent to C_3 . What is the radius of C_4 ?



- (A) $\frac{1}{14}$ (B) $\frac{1}{12}$ (C) $\frac{1}{10}$ (D) $\frac{3}{28}$ (E) $\frac{1}{9}$

- \bigcirc A
- B
- \circ c
- \bigcirc D
- \bigcirc E
- Leave blank (1.5 points)

Not yet answered

Points out of 6

What is the product of all solutions to the equation

$$\log_{7x} 2023 \cdot \log_{289x} 2023 = \log_{2023x} 2023 ?$$

- (A) $(\log_{2023} 7 \cdot \log_{2023} 289)^2$ (B) $\log_{2023} 7 \cdot \log_{2023} 289$ (C) 1
- **(D)** $\log_7 2023 \cdot \log_{289} 2023$ **(E)** $(\log_7 2023 \cdot \log_{289} 2023)^2$

Select one:

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \bigcirc E
- Leave blank (1.5 points)

Question 20

Not yet answered

Points out of 6

Rows 1, 2, 3, 4, and 5 of a triangular array of integers are shown below.

Each row after the first row is formed by placing a 1 at each end of the row, and each interior entry is 1 greater than the sum of the two numbers diagonally above it in the previous row. What is the units digits of the sum of the 2023 numbers in the 2023rd row?

- **(A)** 1

- **(B)** 3 **(C)** 5 **(D)** 7 **(E)** 9

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \bigcirc E
- Leave blank (1.5 points)

Not yet answered

Points out of 6

If A and B are vertices of a polyhedron, define the distance d(A, B) to be the minimum number of edges of the polyhedron one must traverse in order to connect A and B. For example, if AB is an edge of the polyhedron, then d(A,B)=1, but if AC and CB are edges and \overline{AB} is not an edge, then d(A,B)=2. Let Q,R, and S be randomly chosen distinct vertices of a regular icosahedron (regular polyhedron made up of 20 equilateral triangles). What is the probability that d(Q,R) > d(R,S)?

- (A) $\frac{7}{22}$ (B) $\frac{1}{3}$ (C) $\frac{3}{8}$ (D) $\frac{5}{12}$ (E) $\frac{1}{2}$

Select one:

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \bigcirc E
- Contact Con

Question 22

Not yet answered

Points out of 6

Let f be the unique function defined on the positive integers such that

$$\sum_{d|n} d \cdot f\left(rac{n}{d}
ight) = 1$$

for all positive integers n. What is f(2023)?

- (A) 1536 (B) 96 (C) 108 (D) 116

- **(E)** 144

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \cap E
- Leave blank (1.5 points)

Not yet answered

Points out of 6

How many ordered pairs of positive real numbers (a, b) satisfy the equation

$$(1+2a)(2+2b)(2a+b)=32ab$$
?

(A) 0

(B) 1

(C) 2

(D) 3 (E) an infinite number

Select one:

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \bigcirc E
- Control Leave blank (1.5 points)

Question 24

Not yet answered

Points out of 6

Let K be the number of sequences A_1, A_2, \ldots, A_n such that n is a positive integer less than or equal to 10, each A_i is a subset of $\{1,2,3,\ldots,10\}$, and A_{i-1} is a subset of A_i for each i between 2 and n inclusive. For example, $\{\},$ $\{5,7\},$ $\{2,5,7\},$ $\{2,5,7\},$ $\{2,5,6,7,9\}$ is one such sequence, with n=5. What is the remainder when K is divided by 10?

- **(A)** 1
- **(B)** 3
- (C) 5 (D) 7
- **(E)** 9

- \bigcirc A
- \bigcirc B
- \bigcirc C
- \bigcirc D
- \bigcirc E
- Leave blank (1.5 points)

Not yet answered

Points out of 6

There is a unique sequence of integers $a_1, a_2, \dots, a_{2023}$ such that

$$an 2023x = rac{a_1 an x + a_3 an^3 x + a_5 an^5 x + \cdots + a_{2023} an^{2023} x}{1 + a_2 an^2 x + a_4 an^4 x + \cdots + a_{2022} an^{2022} x}$$

whenever an 2023x is defined. What is a_{2023} ?

$$(A) - 2023$$

(A)
$$-2023$$
 (B) -2022 (C) -1 (D) 1 (E) 2023

$$(C) - 1$$

- \bigcirc A
- \bigcirc B
- \circ c
- \bigcirc D
- \bigcirc E
- Leave blank (1.5 points)