

# 2017 AMC 8

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Not yet answered

Points out of 1

Which of the following values is largest?

- (A) 2+0+1+7
- **(B)**  $2 \times 0 + 1 + 7$
- (C)  $2 + 0 \times 1 + 7$
- **(D)**  $2 + 0 + 1 \times 7$
- **(E)**  $2 \times 0 \times 1 \times 7$

Select one:

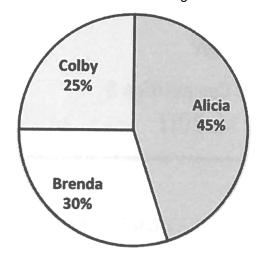
- A
- B
- C
- D
- E

## Question 2

Not yet answered

Points out of 1

Alicia, Brenda, and Colby were the candidates in a recent election for student president. The pie chart below shows how the votes were distributed among the three candidates.



If Brenda received 36 votes, then how many votes were cast all together?

- **(A)** 70
- **(B)** 84
- **(C)** 100
- **(D)** 106
- **(E)** 120

- A
- B
- C
- D
- E

Not yet answered

Points out of 1

What is the value of the expression  $\sqrt{16\sqrt{8\sqrt{4}}}$ ?

- **(A)** 4

- **(B)**  $4\sqrt{2}$  **(C)** 8 **(D)**  $8\sqrt{2}$
- **(E)** 16

Select one:

- A
- B
- C
- D
- $\bigcirc$  E

## Question 4

Not yet answered

Points out of 1

When 0.000315 is multiplied by 7,928,564 the product is closest to which of the following?

- **(A)** 210
- **(B)** 240
- **(C)** 2100
- **(D)** 2400
- **(E)** 24000

Select one:

- A
- B
- C
- D
- E

## Question 5

Not yet answered

Points out of 1

- What is the value of the expression  $\frac{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \cdot 6 \cdot 7 \cdot 8}{1 + 2 + 3 + 4 + 5 + 6 + 7 + 8}?$
- **(A)** 1020
- **(B)** 1120

- **(C)** 1220 **(D)** 2240 **(E)** 3360

- A
- B
- C
- D
- $\bigcirc$  E

Question 6  Not yet answered	_	the degree measures of the angles of a triangle are in the ratio $3:3:4$ , what is the degree easure of the largest angle of the triangle?								
Points out of 1	<b>(A)</b> 18	<b>(B)</b> 36	<b>(C)</b> 60	<b>(D)</b> 72	<b>(E)</b> 90					
	Select one:  A B C									
	) D									
	0 E									
Question <b>7</b> Not yet answered	whose first three digits are the same as its e following numbers must be a factor of $Z$ ?									
Points out of 1	( <b>A</b> ) 11	<b>(B)</b> 19	(C) 101	<b>(D)</b> 111	<b>(E)</b> 1111					
	Select one:									
	<b>A</b>									
	<b>B</b>									
	0 C									
	O D									
	○ E									
Question 8  Not yet answered	Malcolm wants to visit Isabella after school today and knows the street where she lives but doesn't know her house number. She tells him, "My house number has two digits, and exactly three of the following four statements about it are true."									
Points out of 1										
	(1) It is prim	ne.								
	(2) It is eve									
	<ul><li>(3) It is divisible by 7.</li><li>(4) One of its digits is 9.</li><li>This information allows Malcolm to determine Isabella's house number. What is its units digit?</li></ul>									
	(A) 4				(a) 9					
	(A) 4	( <b>B</b> ) 0	(0)1 (	(B) (C)	<i>y</i>					
	Select one:									
	( A									
	<ul><li>○ B</li><li>○ C</li></ul>									
	) D									
	0 E									

Not yet answered

Points out of 1

All of Marcy's marbles are blue, red, green, or yellow. One third of her marbles are blue, one fourth of them are red, and six of them are green. What is the smallest number of yellow marbles that Marcy could have?

- **(A)** 1
- **(B)** 2
- **(C)** 3
- **(D)** 4
- **(E)** 5

Select one:

- A
- B
- C

# Question 10

Not yet answered

Points out of 1

A box contains five cards, numbered 1, 2, 3, 4, and 5. Three cards are selected randomly without replacement from the box. What is the probability that 4 is the largest value selected?

- (A)  $\frac{1}{10}$  (B)  $\frac{1}{5}$  (C)  $\frac{3}{10}$  (D)  $\frac{2}{5}$  (E)  $\frac{1}{2}$

Select one:

- A
- B
- C
- D
- E

#### Question 11

Not yet answered

Points out of 1

A square-shaped floor is covered with congruent square tiles. If the total number of tiles that lie on the two diagonals is 37, how many tiles cover the floor?

- **(A)** 148
- **(B)** 324
- **(C)** 361
- **(D)** 1296
- **(E)** 1369

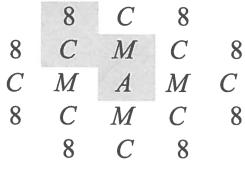
- A
- B
- C
- E

Question 12  Not yet answered	·	The smallest positive integer greater than $1$ that leaves a remainder of $1$ when divided by $4$ , $5$ , and $6$ lies between which of the following pairs of numbers?									
Points out of 1	(A) 2 and 19	<b>(B)</b> 20 and 39	(C) 40 an		( <b>D</b> ) 60 and 79	<b>(E)</b> 80 and 124					
	Select one:										
	○ A										
	○ <b>B</b>										
	○ <b>c</b>										
	○ <b>D</b>										
	○ <b>E</b>										
Question 13		d Kyler played chess nes and lost $3$ games			•	J					
Not yet answered Points out of 1	(A) 0 (B)	_	<b>D</b> ) 3 ( <b>E</b> )	_	ow many games are	no wiii:					
Points out of 1	(, ° ()	- (0)- (	_)	-							
	Select one:										
	<b>A</b>										
	○ B										
	○ <b>C</b>										
	<b>D</b>										
	○ <b>E</b>										
Question 14		e both students in M			= -						
Not yet answered		ms in their homework ad correct answers to	•								
Points out of 1	_	ers were correct. Zoe	-	-							
	alone. What was	Zoe's overall percent	_	nswers?							
	(A) 89 (B	) 92 <b>(C)</b> 93	<b>(D)</b> 96	<b>(E)</b> 98							
	Select one:										
	<ul><li> A</li></ul>										
	○ <b>C</b>										
	O D										
	○ <b>E</b>										

Not yet answered

Points out of 1

In the arrangement of letters and numerals below, by how many different paths can one spell AMC8? Beginning at the A in the middle, a path allows only moves from one letter to an adjacent (above, below, left, or right, but not diagonal) letter. One example of such a path is traced in the picture.



- **(A)** 8
- **(B)** 9
- **(C)** 12
- **(D)** 24
- **(E)** 36

Select one:

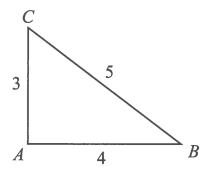
- A
- B
- C
- $\bigcirc$  E

## Question 16

Not yet answered

Points out of 1

In the figure below, choose point D on  $\overline{BC}$  so that  $\triangle ACD$  and  $\triangle ABD$  have equal perimeters.



What is the area of  $\triangle ABD$ ?

- (A)  $\frac{3}{4}$  (B)  $\frac{3}{2}$  (C) 2 (D)  $\frac{12}{5}$  (E)  $\frac{5}{2}$

- A
- B

- E

Not yet answered

Points out of 1

Starting with some gold coins and some empty treasure chests, I tried to put 9 gold coins in each treasure chest, but that left 2 treasure chests empty. So instead I put 6 gold coins in each treasure chest, but then I had 3 gold coins left over. How many gold coins did I have?

- **(A)** 9
- **(B)** 27
- **(D)** 63

**(C)** 45

**(E)** 81

Select one:

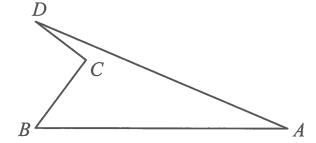
- A
- B
- C
- D
- E

# Question 18

Not yet answered

Points out of 1

In the non-convex quadrilateral ABCD shown below,  $\angle BCD$  is a right angle, AB=12, BC=4, CD=3, and AD=13.



What is the area of quadrilateral ABCD?

- **(A)** 12
- **(B)** 24
- **(C)** 26
- **(D)** 30
- **(E)** 36

- A
- B
- C
- $\bigcirc$  E

Not yet answered

Points out of 1

**(B)** 24 **(A)** 23

**(C)** 25

**(D)** 26

What is the largest integer n for which  $5^n$  is a factor of the sum 98! + 99! + 100!?

For any positive integer M, the notation M! denotes the product of the integers 1 through M.

**(E)** 27

Select one:

- A
- $\bigcirc$  B
- C
- D
- E

## Question 20

Not yet answered

Points out of 1

An integer between 1000 and 9999, inclusive, is chosen at random. What is the probability that it is an odd integer whose digits are all distinct?

(A) 
$$\frac{14}{75}$$

**(B)** 
$$\frac{56}{225}$$

(A) 
$$\frac{14}{75}$$
 (B)  $\frac{56}{225}$  (C)  $\frac{107}{400}$  (D)  $\frac{7}{25}$  (E)  $\frac{9}{25}$ 

**(D)** 
$$\frac{7}{25}$$

**(E)** 
$$\frac{9}{25}$$

Select one:

- A
- B
- C
- E

# Question 21

Not yet answered

Points out of 1

Suppose a, b, and c are nonzero real numbers, and a+b+c=0. What are the possible value(s) for  $\frac{a}{|a|} + \frac{b}{|b|} + \frac{c}{|c|} + \frac{abc}{|abc|}$ ?

- **(A)** 0

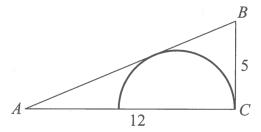
- **(B)** 1 and -1 **(C)** 2 and -2 **(D)** 0, 2, and -2 **(E)** 0, 1, and -1

- A
- B
- C
- E

Not yet answered

Points out of 1

In the right triangle ABC, AC=12, BC=5, and angle C is a right angle. A semicircle is inscribed in the triangle as shown.



What is the radius of the semicircle?

- (A)  $\frac{7}{6}$  (B)  $\frac{13}{5}$  (C)  $\frac{59}{18}$  (D)  $\frac{10}{3}$  (E)  $\frac{60}{13}$

Select one:

- A
- B
- C
- $\bigcirc$  E

## Question 23

Not yet answered

Points out of 1

Each day for four days, Linda traveled for one hour at a speed that resulted in her traveling one mile in an integer number of minutes. Each day after the first, her speed decreased so that the number of minutes to travel one mile increased by 5 minutes over the preceding day. Each of the four days, her distance traveled was also an integer number of miles. What was the total number of miles for the four trips?

- **(A)** 10
- **(B)** 15
- **(C)** 25
- **(D)** 50
- **(E)** 82

- A
- B

- $\bigcirc$  E

Not yet answered

Points out of 1

Mrs. Sanders has three grandchildren, who call her regularly. One calls her every three days, one calls her every four days, and one calls her every five days. All three called her on December 31, 2016. On how many days during the next year did she not receive a phone call from any of her grandchildren?

- **(A)** 78
- **(B)** 80
- (C) 144
- **(D)** 146
- **(E)** 152

Select one:

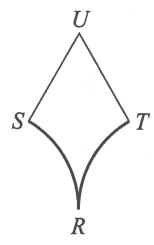
- A
- B
- C
- D
- E

## Question 25

Not yet answered

Points out of 1

In the figure shown,  $\overline{US}$  and  $\overline{UT}$  are line segments each of length 2, and  $m\angle TUS=60^\circ$ .



Arcs  $\widehat{TR}$  and  $\widehat{SR}$  are each one-sixth of a circle with radius 2. What is the area of the region shown?

**(A)** 
$$3\sqrt{3} - \pi$$

**(A)** 
$$3\sqrt{3} - \pi$$
 **(B)**  $4\sqrt{3} - \frac{4\pi}{3}$  **(C)**  $2\sqrt{3}$  **(D)**  $4\sqrt{3} - \frac{2\pi}{3}$  **(E)**  $4 + \frac{4\pi}{3}$ 

**(C)** 
$$2\sqrt{3}$$

$$\textbf{(D)}~4\sqrt{3}-\frac{2\pi}{3}$$

**(E)** 
$$4 + \frac{4\pi}{3}$$

- A
- B
- C
- D
- $\bigcirc$  E